

# PERTURBATION OF NEAR THRESHOLD EIGENVALUES: CROSSOVER FROM EXPONENTIAL TO NON-EXPONENTIAL DECAY LAWS

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For a two-channel model of the form

$$H_\varepsilon = \begin{bmatrix} H_{\text{op}} & 0 \\ 0 & E_0 \end{bmatrix} + \varepsilon \begin{bmatrix} 0 & W_{12} \\ W_{21} & 0 \end{bmatrix} \quad \text{on} \quad \mathcal{H} = \mathcal{H}_{\text{op}} \oplus \mathbf{C},$$

appearing in the study of Feshbach resonances, we continue the rigorous study, begun in our paper [1], of the decay laws for resonances produced by perturbation of unstable bound states close to a threshold. The operator  $H_{\text{op}}$  is assumed to have the properties of a Schrödinger operator in odd dimensions, with a threshold at zero. We consider for  $\varepsilon$  small the survival probability  $|\langle \Psi_0, e^{-itH_\varepsilon} \Psi_0 \rangle|^2$ , where  $\Psi_0$  is the eigenfunction corresponding to  $E_0$  for  $\varepsilon = 0$ . For  $E_0$  in a small neighborhood of the origin *independent of  $\varepsilon$* , the survival probability amplitude is expressed in terms of some special functions related to the error function, up to error terms vanishing as  $\varepsilon \rightarrow 0$ . This allows for a detailed study of the crossover from exponential to non-exponential decay laws, and then to the bound state regime, as the position of the resonance is tuned across the threshold.

*Keywords:* Schrödinger operator, non-exponential decay law, threshold properties

[1] J. Math. Phys. **50** (2009), 013516.